

Cornell Notes

Name Adriana Lopez

Date 9/29/31

Topic Inverse Functions

Class/
Subject Algebra II per. 1 Bonn

7:50 Fermat

$$\begin{aligned} &6-4 \\ \sqrt[3]{y-1} &= \sqrt[3]{32} \\ y-1 &= \sqrt[3]{32} \\ y-1 &= \sqrt[3]{8} \sqrt[3]{4} \\ y+1 &= 2 \sqrt[3]{4} \\ +1 &+1 \end{aligned}$$

$$y = 1 + 2\sqrt[3]{4}$$

8:00 review quiz

8:10 Lesson:

Inverse Functions

$$f(x) = \frac{x-3}{2} \quad g(x) = 2x+3$$

Find inverse using Algebra \longrightarrow

Solve:

A) $2x^4 = 34 \quad | X = \sqrt[4]{17}$

B) $(y-1)^3 = 32$

④ $27^{\frac{4}{3}} = (3^3)^{\frac{4}{3}} = 3^4 = 81$

⑥ $-64^{\frac{2}{3}} = -(4^3)^{\frac{2}{3}} = -(4)^2 = -16$

⑦ $4\sqrt[4]{16} = 2 \frac{(4 \sqrt[4]{3^3})}{\sqrt[4]{3 \sqrt[4]{3^3}}} = 2\sqrt[4]{27}$

⑤ $32^{\frac{3}{5}} = (2^5)^{\frac{3}{5}} = 2^3 = \frac{1}{2^3} = \frac{1}{8}$

⑩ $\left(\frac{12^{\frac{1}{3}}}{4^{\frac{1}{3}}}\right)^2 = \left[\frac{(12)^{\frac{1}{3}}}{4}\right]^2 = (3^{\frac{1}{3}})^2 = 3^{\frac{2}{3}}$

⑫ $\sqrt[3]{(x+1)^3} = \sqrt[3]{18} \rightarrow x = -1 + \sqrt[3]{18}$
 $x+1 = \sqrt[3]{18}$
 $-1 \quad -1$

Using Composition:

Find $F(g(x))$

• these two func. are inverses

Step 1: solve the function for the independent variable (x).

Step 2: Determine if you have a unique solution. \rightarrow

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Topic Inv. Func. continued

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Practice:

* $y = 2x - 4$

- ① solve for x
- ② unique solution?
- ③ switch x & y
- ④ rewrite as inv.

* $f(x) = 2x^2 - 4$

$$y = 2x^2 - 4$$

$$\frac{y+4}{2} = \frac{2x^2}{2}$$

$$\sqrt{\frac{y+4}{2}} = \sqrt{x^2}$$

* $y = \frac{1}{2}x^3 - 2$

$$2(y+2) = \left(\frac{1}{2}x^3\right)2$$

$$\sqrt[3]{2y+4} = \sqrt[3]{x^3}$$

$$x = \sqrt[3]{2y+4}$$

If the solution is unique, the inverse will be a function.
(if solution is unique then inverse IS a function.)

Step 3: Now switch x & y to write inverse.

Step 4: Denote the inverse as y^{-1} or $f^{-1}(x)$

① $\frac{y+4}{2} = \frac{2x}{2} \quad x = \frac{y+4}{2}$

② unique - inv. is func.

③ $y = \frac{x+4}{2}$

④ $y^{-1} = \frac{x+4}{2}$ means inverse of original

① $x = \pm \sqrt{\frac{y+4}{2}}$ ② not unique (+&-)

• inverse is not function

③ $y = \pm \sqrt{\frac{x+4}{2}}$ ④ $f^{-1}(x) = \pm \sqrt{\frac{x+4}{2}}$
inverse

① $x = \sqrt[3]{2y+4}$

② Unique - inverse is func.

③ $y = \sqrt[3]{2x+4}$

④ $y^{-1} = \sqrt[3]{2x+4}$

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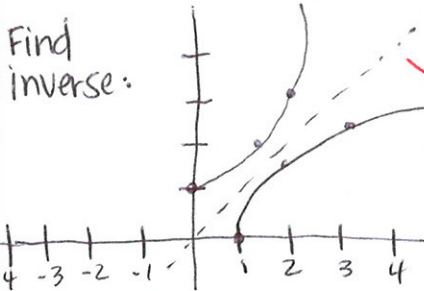
Name Adriana Lopez

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Topic Inv. Func. Continued

Class/Subject Alg. II per. I Bonn

Determine inv. from graph



- we use a vertical line to determine if we have a func.
- We can use a horizontal line to determine if the inverse is a func.

Find Inverse:

- imaginary line
- you can find the inverse by drawing the imaginary line.
- To draw the inverse, count spaces between imaginary line & original line. Then move the same amount of spaces in the opposite direction, plot point, connect points & you have the inverse!

$$f(x) = 2x - 4 \quad g(x) = 3x^2 - 7$$

$$\left(\frac{f}{g}\right)(x) = \frac{2x-4}{3x^2-7}; x \neq \pm\sqrt{\frac{7}{3}}$$

$$3x^2 - 7 = 0$$

+7 +7

$$\frac{3x^2}{3} = \frac{7}{3}$$

$$\sqrt{x^2} = \sqrt{\frac{7}{3}}$$

$$x = \pm \frac{\sqrt{7}}{\sqrt{3}} \quad x = \pm \frac{\sqrt{21}}{3}$$

Homework (6-4) pg. 426-428 #14, 15, 17-23 odd
33-35, 43-47 odd

Home Work ✓ tomorrow

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